## Probability Worksheet



This worksheet allows the calculations of combinations, permutations, random numbers, factorial and probabilities of selected distributions.

## Probability Menu Actions

| [ n ] | Stores the number of total items. |
| :---: | :---: |
| [ r$]$ | Stores the number of items to be taken at a time. |
| [ nCr ] | Calculates the number of combinations. $\mathrm{nCr}=\mathrm{n}!/[\mathrm{r}!\cdot(\mathrm{n}-\mathrm{r})$ ! ] |
| [ nPr ] | Calculates the number of permutations. $\mathrm{nPr}=\mathrm{n}!/(\mathrm{n}-\mathrm{r})$ ! |
| [ RAN\#] | Enters a random number in the range $0 \leq \boldsymbol{x}<1$ |
| N! | Calculates the factorial of the displayed number. |
| [ Select ${ }^{\text {P }}$ <br> Exponential Normal t -Student Weibull | Select one of the available Probability Distribution. |
| [ $p(x)$ ] | Calculates the probability density of the displayed number. |
| [ $p(x)^{-1}$ ] | Calculates the inverse probability density of the displayed number. |
| [ P(x) ] | Calculates the lower-tail cumulative probability of the displayed number. |
| [ P(x) ${ }^{-1}$ ] | Calculates the inverse lower-tail cumulative probability of the displayed number. |

## Example: Combinations

Using 10 colored balls, how many different color combinations of three balls can be chosen?

| Keystrokes | Description |
| :---: | :--- |
| $10[\mathbf{n}]$ | Type the number of total items (10 colored balls). |
| $3[r]$ | Type the size os the sample (3 balls) |
| $[\mathrm{nCr}]$ | Calculate the number of possible combinations. Result $=\mathbf{1 2 0 . 0 0}$ |

## Example: Permutations

Using 5 books labeled A, B, C, D and E, how many different ways can three books be placed on a shelf?

| Keystrokes | Description |
| :---: | :--- |
| $5[\mathbf{n}]$ | Type the number of total items ( 5 books). |
| $3[\mathbf{r}]$ | Type the size os the sample (3 books). |
| $[\mathrm{nPr}]$ | Calculate the number of possible permutations. Result $=\mathbf{6 0 . 0 0}$ |

## Example: Random Number Generator <br> Store a seed value of 42 and generate a sequence of 5 random numbers.

| Keystrokes | Description |
| :---: | :--- |
| 42 [STO] [RAN\#] | Store the initial random seed. |
| $[R A N \#]$ | Generate the 1st random number. Result $=\mathbf{0 . 1 7 0 8}$ |
| $[R A N \#]$ | Generate the 2nd random number. Result $=\mathbf{0 . 7 4 9 9}$ |
| $[R A N \#]$ | Generate the 3rd random number. Result $=\mathbf{0 . 0 9 6 4}$ |
| $[R A N \#]$ | Generate the 4th random number. Result $=\mathbf{0 . 8 7 0 5}$ |
| $[R A N \#]$ | Generate the 4th random number. Result $=\mathbf{0 . 5 7 7 3}$ |

The following examples assumes the "Probability" menu is already visible in the calculator and the display format is set to 6 decimal places.

## Exponential Probability Distribution



When the Exponential probability density function is selected, the distribution "rate parameter" ( $\lambda$ ) can be entered in the corresponding button.

The Probability Density Function is: $\mathbf{p}(\mathbf{x})=\lambda e^{-\lambda x}$

## Example: Exponential Distribution

Consider an Exponential random variable with a rate of 10.

1. What is the probability for a value equal to $0.2 \Rightarrow p(0.2)=$ ?
2. If the probability is $5 \%$, what is the value $\quad \Rightarrow p^{-1}(0.05)=$ ?
3. What is the probability of a value $\leq 0.2 \quad \Rightarrow P(x \leq 0.2)=$ ?
4. What is the value ' $z$ ' for probability of $x \leq z$ is $5 \% \Rightarrow P^{-1}(x \leq z)=0.05$ ?

## Solution:

| Keystrokes | Description |
| :---: | :--- |
| Distribution <br> $[$ Exponential $>]$ | Select the Exponential Probability Distribution |
| $10[\boldsymbol{\lambda}]$ | Type the distribution rate and enter it. |
| $0.2[p(x)]$ | 1) Calculate the probability. Result $=\mathbf{1 . 3 5 3 3 5 3}$ |
| $0.05\left[p(x)^{-1}\right]$ | 2) Calculate the z-value. Result $=\mathbf{0 . 5 2 9 8 3 2}$ |
| $0.2[P(x)]$ | 3) Calculate the probability. Result $=\mathbf{0 . 8 6 4 6 6 5}$ |
| $0.05\left[P(x)^{-1}\right]$ | 4) Calculate the z-value. Result $=\mathbf{0 . 0 0 5 1 2 9}$ |

## Normal Probability Distribution

| n: 10 | r: 3 | nCr | nPr | RAN\# | N! |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Probability Distribution |  |  |  |  |  |
| Norm |  | M: 7.35 |  | $\sigma$ \% 2.33 |  |
| Probability Density |  |  | -ower-Tail Probability |  |  |
| $\mathrm{p}(\mathrm{x})$ | p ( X |  |  |  |  |

When the Normal probability density function is selected, the distribution "mean" $(\mu)$ and standard deviation ( $\sigma$ ) can be entered in the corresponding buttons.

The Probability Density Function is: $\mathbf{p}(\mathbf{x})=$


## Example: Normal Distribution

Consider a Normal random variable with a mean of 7.35 and a standard deviation of 2.33.

1. What is the probability for a value equal to $5.35 \Rightarrow p(5.35)=$ ?
2. IF the probability is $5 \%$, what is the value $\quad \Rightarrow p^{-1}(0.05)=$ ?
3. What is the probability of a value $\leq 5.35 \quad \Rightarrow P(x \leq 5.35)=$ ?
4. What is the value ' $z$ ' for probability of $x \leq z$ is $5 \%=>P^{-1}(x \leq z)=0.05$ ?

## Solution:

| Keystrokes | Description |
| :---: | :--- |
| Distribution <br> $[$ Normal $]$ | Select the Normal Probability Distribution |
| $7.35[\mu], 2.33[\sigma]$ | Input the distribution mean and standard deviation. |
| $5.35[p(x)]$ | 1) Calculate the probability. Result $=\mathbf{0 . 1 1 8 4 5 7}$ |
| $0.05\left[p(x)^{-1}\right]$ | 2) Calculate the z-value. Result $=\mathbf{1 1 . 0 0 5 8 3 7}$ |
| $5.35[P(x)]$ | 3) Calculate the probability. Result $=\mathbf{0 . 1 9 5 3 4 4}$ |
| $0.05\left[P(x)^{-1}\right]$ | 4) Calculate the z-value. Result $=\mathbf{3 . 5 1 7 4 9 1}$ |

## Weibull Probability Distribution

| n : 10 | r: 3 | nCr | nPr | RAN\# | N! |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Probability Distribution |  |  |  |  |  |
| Weib |  | k: 20.0 |  | $\lambda: 100.0$ |  |
| Probability Density |  |  |  |  |  |
| $\mathrm{p}(\mathrm{x})$ | p(x | $\mathrm{P}(\mathrm{x})$ |  | $P(x)^{-1}$ |  |

When the Weibull probability density function is selected, the distribution "shape" parameter (k) and the "scale" parameter ( $\lambda$ ) can be entered in the corresponding buttons.
The Probability Density Function is: $\mathrm{p}(\mathrm{x})=\frac{k}{\lambda}\left(\frac{x}{\lambda}\right)^{k-1} e^{-(x / \lambda)^{k}}$

## Example: Weibull Distribution

Consider a Weibull random variable with a shape factor of 20 and a scale factor of 100 .

1. What is the probability for a value equal to $105 \Rightarrow p(105)=$ ?
2. If the probability is $5 \%$, what is the value $\quad \Rightarrow p^{-1}(0.05)=$ ?
3. What is the probability of a value $\leq 90 \quad \Rightarrow P(x \leq 90)=$ ?
4. What is the value ' $z$ ' for probability of $x \leq z$ is $5 \%=>P^{-1}(x \leq z)=0.05$ ?

## Solution:

| Keystrokes | Description |
| :---: | :--- |
| Distribution <br> $[$ Weibull $]$ | Select the Weibull Probability Distribution |
| $20[k], 100[\lambda]$ | Input the shape $(k)$ and scale $(\lambda)$ parameters of the distribution. |
| $105[p(x)]$ | 1) Calculate the probability. Result $=0.035589$ |
| $0.05\left[p(x)^{-1}\right]$ | 2) Calculate the z-value. Result $=94.584178$ |
| $90[P(x)]$ | 3) Calculate the probability. Result $=\mathbf{0 . 1 1 4 4 7 7}$ |
| $0.05\left[P(x)^{-1}\right]$ | 4) Calculate the z-value. Result $=86.199159$ |

## t-Student Probability Distribution



When the t-Student probability density function is selected, the distribution "Degrees of Freedom" parameter (DF) can be entered in the corresponding button.
The Probability Density Function is: $\mathbf{p}(\mathbf{x})=\frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\sqrt{\nu \pi} \Gamma\left(\frac{\nu}{2}\right)}\left(1+\frac{t^{2}}{\nu}\right)^{-\frac{\nu+1}{2}}$

## Example: Weibull Distribution

Consider a t-Student random variable with 8 degrees of freedom.

1. What is the probability for a value equal to $0.5 \Rightarrow p(0.5)=$ ?
2. If the probability is $5 \%$, what is the value $\quad \Rightarrow p^{-1}(0.05)=$ ?
3. What is the probability of a value $\leq 0.5 \quad \Rightarrow P(x \leq 0.5)=$ ?
4. What is the value ' $z$ ' for probability of $x \leq z$ is $5 \%=>P^{-1}(x \leq z)=0.05$ ?

## Solution:

| Keystrokes | Description |
| :---: | :--- |
| $\left.\begin{array}{c}\text { Distribution } \\ {[t-S t u d e n t}\end{array}\right]$ | Select the t-Student Probability Distribution |
| $8[D F]$ | Input the distribution degrees of freedom. |
| $0.5[p(x)]$ | 1) Calculate the probability. Result $=\mathbf{0 . 3 3 6 6 9 4}$ |
| $0.05\left[p(x)^{-1}\right]$ | 2) Calculate the z-value. Result $=\mathbf{2 . 1 4 5 7 2 4}$ |
| $0.5[P(x)]$ | 3) Calculate the probability. Result $=\mathbf{0 . 6 8 4 7 3 2}$ |
| $0.05\left[P(x)^{-1}\right]$ | 4) Calculate the z-value. Result $=\mathbf{- 1 . 8 5 9 5 4 8}$ |

